Modelling the Partitioning of Evapotranspiration in a Maize-Sunflower Intercrop

C.B.S. Teh, L.P. Simmonds & T.R. Wheeler

1Department of Land Management, Universiti Putra Malaysia
43400 UPM Serdang, Selangor, Malaysia
2Department of Soil Science, University of Reading, Whiteknights
P.O. Box 233, Reading, RG6 6DW, UK
3Department of Agriculture, University of Reading,
Earley Gate P.O. Box 236, Reading, RG6 2AT, UK

ABSTRACT

The primary purpose of this study was to model the partitioning of evapotranspiration in a maize-sunflower intercrop at various canopy covers. The Shuttleworth-Wallace (SW) model was extended for intercropping systems to include both crop transpiration and soil evaporation and allowing interaction between the two. To test the accuracy of the extended SW model, two field experiments of maize-sunflower intercrop were conducted in 1998 and 1999. Plant transpiration and soil evaporation were measured using sap flow gauges and lysimeters, respectively. The mean prediction error (simulated minus measured values) for transpiration was zero (which indicated no overall bias in estimation error), and its accuracy was not affected by plant growth stages, but simulated transpiration during high measured transpiration rates tended to be slightly underestimated. Overall, the predictions for daily soil evaporation were also accurate. Model estimation errors were probably due to the simplified modelling of soil water content, stomatal resistance and soil heat flux as well as due to the uncertainties in characterising the micrometeorological conditions. The SW’s prediction of transpiration was most sensitive to parameters most directly related to canopy characteristics such as the partitioning of captured solar radiation, canopy resistance, and bulk boundary layer resistance.

Keywords: Shuttleworth-Wallace, Penman-Monteith, evapotranspiration, maize, sunflower, intercrop

INTRODUCTION

The Penman-Monteith (PM) model (Monteith 1965) is often used to estimate either the soil evaporation or crop transpiration. Nevertheless, its major drawback is that this model can only be used to estimate either soil evaporation or plant transpiration, but not both simultaneously. Recently, an important extension of the PM model is the Shuttleworth-Wallace (SW) model (Shuttleworth and Wallace 1985). Its improvement over the PM model is that the SW model specifies explicitly the energy exchanges at the soil and canopy, thereby making it possible to distinguish the fraction of water transpired and that evaporated from soil. This means the SW model allows for the interaction between the soil and plant canopy. The SW model, however, was originally developed only for sole crops, and it is still relatively new and not extensively tested (Farahani and Ahuja 1996). Nevertheless, the few field
tests of this model in both agricultural and non-agricultural conditions have been promising (Lafleur and Rouse 1990; Wallace et al. 1990; Stannard 1993; Farahani and Bausch 1995). Stannard (1993), for example, observed that predictions from the SW model were significantly more accurate than the PM model when applied in very sparse canopies (leaf area index < 0.2).

The objectives of this study were two-fold. Firstly, it was to model the partitioning of evapotranspiration in a maize-sunflower intercropping system in partial- and fully-grown canopies. This would be achieved by extending the original SW model to intercropping systems. Secondly, this study aimed to determine accuracy and perform a sensitivity analysis of the extended SW model when applied in the maize-sunflower intercrop.

MODEL DEVELOPMENT
The SW model was extended to include the transpiration from two or more crops and evaporation from the soil. This extension of including evapotranspiration from $n$ crop species (with soil interaction) was first shown by Wallace (1997). Fig. 1 shows how the resistance to the fluxes of radiation, latent and sensible heat is distributed in the soil-plant-atmosphere system involving two crop species. The energy budget of the system is described in a series of equations, which are the sum of the various latent heat, sensible heat and radiation fluxes. With some algebraic manipulations, it can be shown that the total latent heat flux of the system with $n$ crops is given by

$$\lambda E = \sum_{i=1}^{n} C_{c,i} PM_{c,i} + C_s PM_s$$

where

$$PM_{c,i} = \frac{\Delta A + \left\{ \rho c_p D - \Delta r_s^{ci} \left( A - A_{c,i} \right) \right\} / \left( r_a^o + r_s^{ci} \right)}{\Delta + \gamma \left\{ 1 + r_s^{ci} / \left( r_a^o + r_s^{ci} \right) \right\}}$$

$$PM_s = \frac{\Delta A + \left\{ \rho c_p D - \Delta r_s^s \left( A - A_s \right) \right\} / \left( r_a^o + r_s^s \right)}{\Delta + \gamma \left\{ 1 + r_s^s / \left( r_a^o + r_s^s \right) \right\}}$$

$$C_{c,i} = \left( \frac{1}{R_s} + \sum_{j=1, j \neq i}^{n} \frac{1}{R_{c,j}} \right)^{-1}$$

$$1 + \left( \frac{1}{R_{c,i}} + \frac{1}{R_a} \right)^{-1}$$

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Fig. 1: Schematic diagram of the various energy fluxes, temperatures, vapour pressures and resistances in a two-crop intercropping system. Key: $\lambda E$, $\lambda E_{c,1}$, $\lambda E_{c,2}$ and $\lambda E_s$ are latent heat fluxes from the system, first crop, second crop and soil, respectively; $H$, $H_{c,1}$, $H_{c,2}$ and $H_s$ are sensible heat fluxes from the system, first crop, second crop and soil, respectively; $R_a$ and $R_{a'}$ are net radiation fluxes into the system and to the soil, respectively; $G$ is heat conduction into the soil; $T_r$, $T_{f,1}$, $T_{f,2}$, $T_s$ and $T$ are temperatures for the reference height, first crop, second crop, mean canopy flow (canopy source height) and soil, respectively; $e_s$ and $e_{r,1}$ are vapour pressure at the reference height and mean canopy flow, respectively; $e_s(T)$ is saturated vapour pressure at temperature $T$; $r_a^{1}$ is aerodynamic resistance between the mean canopy flow and reference height; $r_a^{1}$ and $r_a^{2}$ are bulk stomatal resistance for the first crop and second crop, respectively; $r_{a,1}$ and $r_{a,2}$ are bulk boundary layer resistance of the canopy for the first crop and second crop, respectively; $r_s$ is aerodynamic resistance between the soil and mean canopy flow; and $r_s'$ is soil surface resistance.

\[
C_s = \left\{1 + R_s R_a / R_c \left( R_s + R_a \right) \right\}^{-1}
\]

\[
R_{c,i} = (\Delta + \gamma) r_a^{c,i} + \gamma r_s^{c,i}
\]

\[
R_a = (\Delta + \gamma) r_a^{a}
\]

\[
R_s = (\Delta + \gamma) r_a^{s} + \gamma r_s^{s}
\]

where $c_p$ is the specific heat of water at constant pressure (4182 J kg$^{-1}$ K$^{-1}$); $D$ is the vapour pressure deficit, or $e_s(T_r) - e_{r,1}$; $\Delta$ is the mean rate of change of saturated vapour pressure with temperature, or \[e_s(T_r) - e_{r,1}] / (T_r - T_0)\); $\gamma$ is the psychrometric constant (0.658 mb K$^{-1}$); $A$ and $A_i$ are the total energy available to the system and soil, respectively, and $A_{c,i}$ is the amount of energy available to crop $i$ so that:
Eq. 2: Comparison between simulated and measured transpiration for the intercrop components in the 1998 and 1999 experiments: (a) maize, and (b) sunflower

\[ A_{c,i} = F_i R_n \]  \hspace{1cm} (6)

where \( F_i \) is the fraction of radiation intercepted by crop species \( i \). \( F_i \) is determined from the plant-radiation model developed by Spitters (1989), and Kustas and Norman (1999a; 1999b). The energy available to the soil \( A_s \) is:

\[ A_s = (R_n - G) \cdot \left(1 - \sum_{i=1}^{n} F_i \right) \]  \hspace{1cm} (7)

Note that Eq. (3) is a correction to the equation given in Wallace (1997). The original equation erroneously excluded the \( 1/R_s \) term, and showed that the summation of \( 1/R_{c,j} \) is over \( j = 2 \) to \( n \), which ought to be over \( j = 1 \) to \( n \) excluding \( j = i \).

The partitioning of the various latent heat fluxes is determined from the total latent heat flux \( \lambda E \) which is the sum of all latent heat fluxes in the intercropping system, or in a two-crop intercropping system:

\[ \lambda E = \lambda E_s + \lambda E_{c,1} + \lambda E_{c,2} \]

\[ = \frac{\Delta A_s + \left( \rho c_p D_0 \right) / r_a^s}{\Delta + \gamma \left(1 + r_i^s / r_a^s \right)} + \frac{\Delta A_{c,1} + \left( \rho c_p D_0 \right) / r_a^{c,1}}{\Delta + \gamma \left(1 + r_i^{c,1} / r_a^{c,1} \right)} + \]

\[ \frac{\Delta A_{c,2} + \left( \rho c_p D_0 \right) / r_a^{c,2}}{\Delta + \gamma \left(1 + r_i^{c,2} / r_a^{c,2} \right)} \]  \hspace{1cm} (8)
where $D_v$ is the vapour pressure deficit at the canopy source height, or

$$D_v = D + \frac{r_a^a}{\rho C_p} \left\{ \Delta A - (\Delta + \gamma) \Delta E \right\}$$  \hspace{1cm} (9)

The SW model required several resistance components to be known. These are: $r_a^a$ (resistance between mean canopy flow and reference height); $r_s^b$ (bulk stomatal resistance); $r_c^b$ (bulk canopy boundary layer resistance); $r_a$ (resistance between soil and mean canopy flow); and $r_s$ (soil surface resistance). The calculations for these resistance components were obtained from Choudhury and Monteith (1988) and Shuttleworth and Gurney (1990). A crop’s stomatal resistance $r_s$ was assumed to be related only to PAR (photosynthetically active radiation). This relationship is described by

$$\frac{1}{r_s^b} = \frac{a_1 \cdot I_{PAR}}{a_2 + I_{PAR}}$$  \hspace{1cm} (10)

where $I_{PAR}$ is the PAR irradiance; and $a_1$ and $a_2$ are the empirical coefficients (Jarvis 1976). Bulk stomatal resistance is determined simply by

$$r_s^b = \frac{R_s^i}{L}$$  \hspace{1cm} (11)

(Thom 1972; Shuttleworth 1978; Stannard 1993).

Finally, heat flux into the soil $G$ is calculated by

$$G = 0.35 \cos \theta \cdot R_s^i$$  \hspace{1cm} (12)

where soil heat flux was simply a fraction (0.35) of the radiation reaching the soil surface (Kustas and Norman 1999a; 1999b).

**MATERIALS AND METHODS**

Maize (*Zea mays* L. cv. Hudson) and sunflower (*Helianthus annuus* L. cv. Sanluca) were sown on 22 May 1998 at Sonning Farm (51°27’ N and 0°58’ W). The soil was a deep, freely draining soil, brown to grey-brown, and having clay and sand contents of 17% and 69%, respectively. Soil pH was 4.5 to 7.0; organic matter content was 1.5 to 2.0%; and bulk density was 1.67 Mg m$^{-3}$. Total field size was 0.13 ha, and planting rows were in a NE-SW direction. Inter-row distance was 0.6 m, but intra-row planting distance for maize was 0.3 m and for sunflower it was 0.6 m, so that the ratio of maize to sunflower was 2:1. The planting density of maize was 3 plants m$^{-2}$, and 1.5 plants m$^{-2}$ for sunflower. Thirty days after sowing, fertilisers were applied at rates of 120 kg ha$^{-1}$ N, 200 kg...
ha⁻¹ P₂O₅, and 200 kg ha⁻¹ K₂O. No herbicides or pesticides were applied; weeding was manual; and the crops were entirely rain-fed.

Data collection started 66 days after sowing (DAS 66), and continued every five to nine days for 30 days. The LAI (leaf area index) was measured using a leaf area machine (LI-COR, Lincoln, Nebraska, USA; Model 3000); solar irradiance by a sunfleck ceptometer (Decagon Devices Inc., Pullman, Washington, USA; Model SF-80); stomatal resistance by an infrared gas analyser (CIRAS, PP Systems, Hitchin Hertfordshire, UK); and soil evaporation by lysimeters, measuring 50 mm in diameter and 120 mm in depth. Plant transpiration or sap flow was measured using customised sap flow gauges based on the concept of stem heat balance (Sakuratani 1981), where the principle is to apply a known rate of heat into a stem segment, then partition the heat input between conductive and convective losses, where the latter is proportional to the volumetric sap flux up the stem. Lastly, daily and half hourly weather data (air temperature, total incoming radiation, wind speed and vapour pressure) were obtained from an automatic weather station at Sonning Farm.

The exact same field experiment as in 1998 was conducted again in 1999. Maize and sunflower were planted on 28 May 1999 at Sonning Farm. The same planting densities, planting row direction, field maintenance and data collection as in the 1998 experiment were repeated for this year. Data collection in the 1999 experiment, however, started on DAS 33, and continued every five to nine days for 35 days.

**RESULTS AND DISCUSSION**

*Plant Transpiration*

Overall, the SW model predicted the transpiration of the intercrop components with reasonable accuracy (Table 1 and Fig. 2). There was a close clustering of points along the 1:1 line of equality, and their mean errors were zero, which indicated no overall bias in estimation errors. Moreover, 95% of these errors occurred in a narrow range within -0.08 to 0.07 mm h⁻¹. Nevertheless, the SW model tended to underestimate transpiration slightly for intercrop maize and intercrop sunflower when measured transpiration rates were high, when exceeding 0.15 and 0.40 mm h⁻¹, respectively (Fig. 2).

*Figs. 3 and 4* show the diurnal transpiration rates for the intercrop components on some selected days. Transpiration rates usually increased from morning, reaching a maximum at about 12:00 to 14:00 hours, then decreased towards late evening. This observed diurnal trend of transpiration generally followed the measured diurnal trend of temperature, solar irradiance and vapour pressure deficit (Ozier-Lafontaine *et al.* 1997). There was overall good agreement between the diurnal simulated and measured transpiration values. Overall, the SW model predicted the partitioning of transpiration between maize and sunflower in the intercropping system with reasonable accuracy. The accuracy of the SW model was quite robust to the different plant growing stages. It gave reasonable estimations throughout the growing season although: i) stomatal resistance was only related to PAR irradiance (Eq. 10), ii)
there was no modelling of soil water movement and content, and iii) only simplified modelling of soil heat flux (Eq. 12) was undertaken.

In this study, stomatal resistance was only related to PAR irradiance, omitting the effects of other important factors such as air temperature, vapour pressure deficit, CO₂ concentration, and soil water content (Jarvis 1976). In addition, the crops in this study were only rain-fed; consequently, it is reasonable to expect that there might be periods on hot, sunny days when plants could be water-stressed and develop water deficit in leaves. Furthermore, this study did not model soil water movement but assumed that the soil was always at field capacity (volumetric water content of 0.22 m³ m⁻³). These reasons could explain why the SW model tended to slightly underestimate transpiration during high measured transpiration rates.

One possible source of error was the simplified modelling of heat flux into the soil. Soil heat flux was assumed to be only a fraction of solar irradiance reaching the soil surface, and this fraction was diurnally varied. Kustas et al. (1989) found that between 9:00 to 16:00 hours the ratio of soil heat flux to solar irradiance reaching the soil surface was 0.35. Jones (1991) stated that the ratio of soil heat flux to solar irradiance could vary from 0.02 for dense canopies to more than 0.30 for sparse canopies. This ratio is also dependent on soil properties such as soil moisture. Accuracy of simulations could be improved by incorporating a soil water transport model to estimate more precisely the canopy and soil resistance, and the soil heat flux and evaporation.

Errors or uncertainties in characterising the micrometeorological conditions of each crop species may be another source of error. Uncertainties, especially for intercropping systems, occur because no satisfactory method exists for simulating the convective transfer inside heterogeneous canopies, and that the intercepted radiation is highly variable within canopies (Gijzen and Goudriaan 1989; Tournebize et al. 1996). It would be difficult to characterise the large variability of
Fig. 3: Comparison between simulated and measured diurnal transpiration for the intercrop maize: (a) DAS 71, 1998; (b) DAS 78, 1998; (c) DAS 95, 1998; (d) DAS 42, 1999; (e) DAS 44, 1999; and (f) DAS 53, 1999.
Fig. 4: Comparison between simulated and measured diurnal transpiration for the intercrop sunflower: (a) DAS 71, 1998; (b) DAS 78, 1998; (c) DAS 95, 1998; (d) DAS 42, 1999; (e) DAS 44, 1999; and (f) DAS 53, 1999.
TABLE 1
Simulation error of transpiration (mm h⁻¹)

<table>
<thead>
<tr>
<th>Intercrop component</th>
<th>Mean Error (simulated – measured)</th>
<th>Mean – 2SD</th>
<th>Mean + 2SD</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maize</td>
<td>0.00</td>
<td>-0.06</td>
<td>0.05</td>
</tr>
<tr>
<td>Sunflower</td>
<td>0.00</td>
<td>-0.08</td>
<td>0.07</td>
</tr>
</tbody>
</table>

SD - standard deviation

![Graph](image)

*Fig. 5: Comparison between simulated and measured daily soil evaporation: (a) 1998 experiment, and (b) 1999 experiment*

microclimatological parameters within canopies by only using the meteorological data collected above the canopies as was done in this study. Some studies indicated that air-flow and temperature distributions for row crops were likely to differ from profiles in vegetation randomly distributed in aerial space (Arkin and Perrier 1974; Graser et al. 1987), especially when furrow depth (height) and plant spacing was large relative to vegetation height and amount of cover (Graser et al. 1987; Kustas et al. 1989). Observations from Ham and Heilman (1991) indicated that soil and
aerodynamic resistance was not significantly related to meteorological conditions above the canopy. They concluded that approaches using bulk aerodynamic resistance with standard meteorological data were not appropriate for sparse canopies, and that the gradient-driven transport, or the so-called K-theory, was not applicable. The use of K-theory has always been controversial because of its lack of a strong theoretical basis. Contrary to the study by Ham and Heilman (1991), several studies were successful in applying K-theory for sparse canopies (Dolman and Wallace 1991; Nichols 1992; Flerchinger et al. 1998). Another possible source of error in this study was the risk of advection due to the heterogeneous canopies and due to field sizes that may not be sufficiently large enough (Tournebize et al. 1996). More complete micrometeorological profiles would be required to overcome these shortcomings (Ozier-Lafontaine et al. 1997).

**Daily Soil Evaporation**

Simulations followed the observed trend of daily soil evaporation quite closely (Fig. 5). In the 1998 experiment. For example, daily soil evaporation increased from DAS 70 to 75, and decreased from DAS 78 to 84. Simulations likewise showed the same increasing and decreasing patterns for DAS 70 to 75 and DAS 78 to 84, respectively. Mean estimation error was 0.02 mm day$^{-1}$ with 95% error band within $-0.80$ to $-0.85$ mm day$^{-1}$.

There were larger errors in predictions for the daily soil evaporation than for plant transpiration. For greater accuracy in estimating daily soil evaporation, incorporating a soil water model is warranted for both models. Soil water was
always assumed at field capacity, and soil water changes due to rainfall and water movement were neglected in this study. The absolute amount of soil evaporation depends on the available energy at the soil surface (which is strongly related to canopy cover), frequency of soil wetting and soil type (Thornley 1976; Wallace et al. 1990; 1991).

**Sensitivity Analyses**

Fig. 6 illustrates the sensitivity of simulated transpiration by maize and sunflower in the intercropping system to model parameters such as the crop captured radiation $A_{c, a}$, canopy resistance $r_{c, a}^c$, bulk boundary layer resistance $r_{a, b}^c$, aerodynamic resistance between canopy source height and reference level $r_{a, b}^r$, vapour pressure deficit at canopy source height $D_p$, and volumetric soil water content $\Theta$. These results of sensitivity analyses were simulated for 12:00 hours on DAS 72, 1998, where the average half-hourly values for total incoming radiation was 689 W m$^{-2}$, air temperature was 17°C, wind speed was 1.6 m s$^{-1}$, and vapour pressure was 20 mb. Sensitivity analyses were also done for various plant growth stages, for various daylight hours and for other days, and the results obtained were similar to the results shown in Fig. 6. Other model parameters were also tested such as the aerodynamic resistance between the soil surface and canopy source height $r_{a, c}^s$, soil surface resistance $r_{a, s}^s$, and soil heat flux $G$. Nevertheless, these model parameters produced less than 1% change in transpiration even at 20% change in the model parameters; thus, transpiration was regarded as insensitive to these model parameters.

Simulated transpiration for both crops was most sensitive to $A_{c, a}$ followed by $r_{a, b}^c$ and $r_{c, a}^c$. These three model parameters were more directly related to canopy characteristics than other model parameters. The importance of $A_{c, a}$, $r_{a, b}^c$, and $r_{c, a}^c$ highlighted the importance of determining accurately, for each crop species in the system, the fraction of incident radiation intercepted, the canopy resistance, and the bulk canopy boundary layer resistance. It is not surprising that plant transpiration would be sensitive to canopy resistance $r_{c, a}^c$, considering that water would evaporate from the plant mainly through the stomatal openings. Shuttleworth and Wallace (1985) noted that bulk canopy boundary layer resistance $r_{c, a}^d$ was usually significant when acting in combination with much larger canopy resistance. Sensitivity analyses done by Shuttleworth and Wallace (1985) for a monocrop system revealed that transpiration was insensitive to $r_{a, b}^c$; changing $r_{a, b}^c$ by a factor of two did not change transpiration by more than 2%. In this study, a 20% change in $r_{c, a}^c$ for a two-crop intercropping system produced a maximum of about 8% change in transpiration.

**CONCLUSION**

This study successfully extended and applied the SW evapotranspiration model to intercropping systems. Mean errors were zero and errors were limited to a narrow 95% range. Model accuracy was robust to the different plant growth stages or canopy cover. However, the SW model tended to slightly underestimate
transpiration when the measured transpiration rates were high. For the sunflower
and maize components in intercrop, it tended to underestimate slightly when
measured transpiration rate exceeded 0.40 mm h\textsuperscript{-1} and 0.15 mm h\textsuperscript{-1}, respectively.

There were larger errors in predictions for the daily soil evaporation than for
plant; moreover soil water content was assumed to be always at field capacity.
Simulations nevertheless followed the daily trend of soil evaporation closely.

Finally, sensitivity analyses revealed that modelling plant transpiration was
most sensitive to model parameters most directly related to canopy characteristics.
It was most sensitive to the partitioning of captured radiation among crops $A_{c,n}$,
canopy resistance $r_{c,i}$, and bulk boundary layer resistance $r_{g,b}$.

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